Constrained Deep Reinforcement Learning for Energy Sustainable Multi-UAV Based Random Access IoT Networks With NOMA

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Abstract-In this paper, we apply the Non-Orthogonal Multiple Access (NOMA) technique to improve the massive channel access of a wireless IoT network where solar-powered Unmanned Aerial Vehicles (UAVs) relay data from IoT devices to remote servers. Specifically, IoT devices contend for accessing the shared wireless channel using an adaptive p-persistent slotted Aloha protocol; and the solar-powered UAVs adopt Successive Interference Cancellation (SIC) to decode multiple received data from IoT devices to improve access efficiency. To enable an energy-sustainable capacity-optimal network, we study the joint problem of dynamic multi-UAV altitude control and multi-cell wireless channel access management of IoT devices as a stochastic control problem with multiple energy constraints. We first formulate this problem as a Constrained Markov Decision Process (CMDP), and propose an online model-free Constrained Deep Reinforcement Learning (CDRL) algorithm based on Lagrangian primal-dual policy optimization to solve the CMDP. Extensive simulations demonstrate that our proposed algorithm learns a cooperative policy in which the altitude of UAVs and channel access probability of IoT devices are dynamically controlled to attain the maximal long-term network capacity while ensuring energy sustainability of UAVs, outperforming baseline schemes. The proposed CDRL agent can be trained on a small network, yet the learned policy can efficiently manage networks with a massive number of IoT devices and varying initial states, which can amortize the cost of training the CDRL agent.

Index Terms—Constrained deep reinforcement learning, UAV altitude control, solar-powered UAVs, energy sustainable IoT networks, *p*-persistent slotted Aloha, non-orthogonal multiple access.

I. INTRODUCTION

WHILE internet connectivity plays an increasing role in people's everyday life in densely populated areas, some rural areas and nature fields such as farms, deserts, oceans,

Manuscript received January 31, 2020; revised June 7, 2020; accepted July 19, 2020. Date of publication August 25, 2020; date of current version March 17, 2021. This work was supported in part by the NSF under Grant ECCS-1554576, Grant ECCS-1610874, and Grant CNS-1816908; and in part by the U.S. Department of Energy, Office of Science, under Contract DE-AC02-06CH11357. (*Corresponding author: Sami Khairy.*)

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Digital Object Identifier 10.1109/JSAC.2020.3018804

and polar regions, typically lack expansive internet coverage. This is because network providers tend to deploy telecommunication infrastructure in areas where providing wireless service is economically profitable. Nevertheless, farmers, environmental agencies, research organizations, defense agencies, and utility companies among many others, have increasing demands for internet connectivity in such under-served areas, to support massive Internet of Things (IoT) based applications ranging from tracking animal health, agricultural growth, and marine life, to surveillance sensors for defense applications and nuclear waste site management, just to name a few. Provisioning wireless internet access for a massive number of IoT devices in under-served areas at cost effective rates is undoubtedly of great interest for governments, businesses, and end customers.

With the explosive growth of IoT based applications, new distributed channel access and coverage solutions should be conceived. Distributed random access based wireless technologies such as Wi-Fi, Zigbee, and Aloha-based Long Range Wide Access Networks (LoRaWAN), will inevitably play an important role in provisioning massive IoT access in 5G systems and beyond, due to their scalability and ease of implementation [1]-[4]. In fact, the recent decision by the Federal Communications Commission (FCC) to open the 6GHz band for unlicensed use [5], further promotes random access based unlicensed wireless networks and renders them as an integral part of the beyond 5G wireless network ecosystem. Non Orthogonal Multiple Access (NOMA), which can improve the access efficiency by exploiting Successive Interference Cancellation (SIC) to enable non-orthogonal data transmissions, is yet another promising solution to enable massive machine type communication (mMTC) in 5G networks and beyond. Recent works propose to apply power-domain NOMA in slotted-Aloha systems to support mMTC of IoT devices [6]-[8].

On the other hand, Unmanned Aerial Vehicle (UAV) based wireless relays have been recently proposed as a new on-demand coverage solution to facilitate fast and flexible deployment of communication infrastructure [9]–[17]. UAVs, especially those in the form of quadcopter drones, can be used as aerial base stations within a 5G network to provision wireless internet connectivity to IoT devices in remote areas, or enhance wireless system capacity, reliability, and energy efficiency, in urban areas, by relaying data to network servers

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through satellite back-haul links [18], [19]. Furthermore, UAVs equipped with wireless transceivers can dynamically adjust their location in real-time to counter environmental changes and improve system performance. UAVs, however, are battery operated which constrains the operation time of the network device. One promising direction to extend the operation time of the network is to devise solar-powered UAVs which can harvest solar energy from the sun [20], [21]. In this case, the system controller is also tasked with managing the energy evolution process of the UAV battery to ensure energy efficiency or sustainability.

In this work, we consider solar-powered multi-UAV based wireless IoT networks, where UAVs act as wireless Base Stations (BS) for a massive number of IoT devices. IoT devices contend for access to the shared wireless channel using an adaptive p-persistent slotted Aloha MAC protocol to send data to the UAVs, which relay the received data to the internet backbone through wireless satellite back-haul links. UAVs on the other hand, are equipped with solar cells to replenish the on-board battery, and exploit power-domain SIC to decode multiple users' transmissions, thus improving the transmission efficiency. To enable an energy-sustainable and capacity-optimal massive IoT network, we study the joint problem of dynamic multi-UAV altitude control and NOMAbased multi-cell wireless channel access management of IoT devices. The objective of the stochastic control problem is to maximize the total network capacity of a massive number of IoT devices which is characterized by random uplink channel access, varying wireless channel conditions, and dynamic network topology, while satisfying multiple constraints to ensure energy sustainability of solar-powered UAVs. To the best of our knowledge, our work is the first work to study energy sustainability of a multi-UAV based wireless communication system in support of a massive number of IoT devices with NOMA and random channel access.

The main contributions of our work can be summarized as follows. First, we formulate the joint problem of multi-UAV altitude control and adaptive random channel access of massive IoT devices to attain the maximum capacity under energy sustainability constraints of UAVs over a prespecified operating horizon as a Constrained Markov Decision Process (CMDP). Second, to learn an optimal control policy for the wireless communication system, we design an online model-free Constrained Deep Reinforcement Learning (CDRL) algorithm based on Lagrangian primal-dual policy optimization to solve the CMDP. It is shown that the proposed CDRL agent learns a cooperative policy among UAVs which ensures their energy sustainability over the operating horizon, while maximizing the total network capacity under the probabilistic mutual interference of IoT devices. Third, to evaluate the effects of policy optimization in our proposed CDRL framework, we compare the learning performance with two other DRL agents which adopt different policy optimization algorithms, namely, Trust Region Policy Optimization (TRPO) [22], and Vanilla Policy Gradient (VPG) [23]. It is shown that our proposed CDRL agent which combines Lagrangian primal-dual optimization techniques with Proximal Policy Optimization (PPO) [24] outperforms other agents in terms of both the achieved rewards

and constraint satisfaction. In addition, we compare the performance of the learned policy to three baseline policies learned by a 1) Deep RL (DRL) agent which is energy-unaware, a 2) DRL agent which adopts reward shaping to penalize energy dissipation, and 3) a random management policy. Compared with baseline policies, our extensive simulations demonstrate that our proposed CDRL agent learns a feasible adaptive policy which achieves a temporal average network capacity that is 81% higher than that of a feasible DRL agent with reward shaping, and only 6.7% lower than the upper bound achieved by the energy-unaware DRL agent. Last but not least, we demonstrate that the learned policy, which has been efficiently trained on a small network size, can effectively manage networks with a massive number of IoT devices and varying initial network states.

The remainder of this paper is organized as follows. A literature survey of related research work and a background of unconstrained and constrained MDPs is given in Section II. The system model is described in Section III. The problem formulation and the proposed CDRL algorithm is presented in Section IV, followed by the simulation setup and performance evaluation results in Section V. Finally our concluding remarks and future work are given in Section VI.

II. BACKGROUND AND RELATED WORKS

A. UAV Based Wireless Networks

The deployment and resource allocation of UAV-based wireless networks has been studied in many works. In [9], a polynomial-time algorithm is proposed for successive UAV placement such that the number of UAVs required to provide wireless coverage for a group of ground terminals is minimized and each ground terminal is within the communication range of at least one UAV. The downlink coverage probability for UAVs as a function of the altitude and antenna gain is analyzed in [10]. Based on the circle packing theory, the 3D locations of the UAVs are determined to maximize the total coverage area while ensuring the covered areas of multiple UAVs do not overlap. The work of [11] studies the problem of multiple UAV deployment for on-demand coverage while maintaining connectivity among UAVs. In [12], a distributed coverage-maximizing algorithm for multi UAV deployment subject to the constraint that UAVs maintain communication is proposed for surveillance and monitoring applications.

3D trajectory design and resource allocation in UAV based wireless networks have also been studied in [13]–[17]. In [13], a mixed integer non-convex optimization problem is formulated to maximize the minimum downlink throughput of ground users by jointly optimizing multi-user communication scheduling, association, UAVs' 3D trajectory, and power control. An iterative algorithm based on block coordinate descent and successive convex optimization techniques is proposed to solve the formulated problem. Reference [14] extends on [13] by considering heterogeneous UAVs so that each UAV can be individually controlled. Machine learning based approaches have also been recently considered for UAV 3D trajectory design. In [15], the flight trajectory of the UAV and scheduling of packets are jointly optimized to minimize the sum of Age-of-Information (sum-AoI) at the UAV. The problem is modeled as a finite-horizon Markov Decision Process (MDP) with finite state and action spaces, and a DRL algorithm is proposed to obtain the optimal policy. Reference [16] devises a machine learning based approach to predict users' mobility information, which is considered in the trajectory design of multiple UAVs. A sense-and-send protocol is designed in [17] to coordinate multiple UAVs, and a multi-UAV Q-learning based algorithm is proposed for decentralized UAV trajectory design. Scheduling based NOMA systems with a UAV-based BS to serve terrestrial users are considered in [25], [26]. In a recent work, the performance of NOMA transmissions in a single-hop random access wireless network is investigated, and an iterative algorithm is proposed to find the optimal transmission probabilities of users to achieve the maximum throughput [27]. Furthermore, the control, motion planning, and aerodynamic power consumption of UAVs have been studied in [28]-[30].

It is worth to mention that all aforementioned works consider battery powered UAVs with limited energy storage capacity, which constrains the operating horizon. Solar-powered UAVs have great potential to extend the operation time by harvesting solar energy from the sun [20], [21]. Reference [31] studies the optimal trajectory of solar-powered UAVs for maximizing the solar energy harvested. In their design, a higher altitude is preferable to maximize harvested energy. On the other hand, [32] studies the trade-off between solar energy harvesting and communication system performance of a single UAV based wireless network. It is shown that in order to maximize the system throughput, the solar-powered UAV climbs to a high altitude to harvest enough solar energy, and then descends to a lower altitude to improve the communication performance.

The work of [32] considers downlink wireless resource allocation in a centralized scheduling-based and interferencefree wireless network with a single UAV. Deploying one solarpowered UAV may lead to a communication outage when the UAV ascends to high altitudes to replenish its on-board battery, and therefore, one UAV cannot satisfactorily serve wireless users and ensure its energy sustainability. On the other hand, scheduling-based networks usually suffer from the curse of dimensionality and do not scale well to massive IoT networks, as signaling overheads scale up with the network size. This has led to a growing interest in wireless networks with NOMA and distributed random access based Medium Access Control (MAC) protocols, such as Aloha-type MAC adopted in LoRaWAN networks [4]. It is very challenging to analyze the performance of distributed multi-cell random access networks with NOMA-enabled aerial base stations due to the combinatorial space of possible transmissions and interference that affect decoding events, and the time varying network topology. Machine learning provides a data driven approach for end-to-end system design, and can be therefore used to holistically study these challenging wireless systems and provide proper guidance for integration within 5G systems and beyond. In this work, we study solar-powered multi-UAV based massive IoT networks with random-access and NOMA, and propose solutions to ensure long-term energy sustainability of UAVs without causing wireless service interruption or degradation. Specifically, we propose a new framework for data-driven stochastic control under constraints, by combining DRL policy optimization methods with Lagrangian primaldual optimization, and apply it to the problem of multi-UAV altitude control and wireless random channel access management. Our proposed solution demonstrates that by deploying multiple UAVs, it is possible to learn a cooperative policy in which multiple UAVs take turns to charge their battery and provision uninterrupted wireless service to IoT devices.

B. Constrained Deep Reinforcement Learning

One of the primary challenges faced in reinforcement learning is the design of a proper reward function which can efficiently guide the learning process. Many real world problems are multi-objective problems in which conflicting objectives should be optimized. A common approach to handling multiobjective problems in RL is to combine the objectives using a set of coefficients [33]. With this approach, there exist a set of optimal solutions for each set of coefficients, known as the Pareto optimal solutions [34]. In practice, finding the set of coefficients which leads to the desired solutions is not a trivial task. For many problems, it is more natural to specify a single objective and a set of constraints. The CMDP framework is the standard formulation for RL problems involving constraints [35]. Optimal policies for CMDPs can be obtained by solving an equivalent linear programming formulation [35], or via multi time-scale dynamic-programming based algorithms [36]-[40]. Such methods may not be applicable to large scale problems or problems with continuous stateaction space. Leveraging recent advances in deep learning and policy search methods [22], some works devise multi-time scale algorithms for solving RL problems in presence of constraints [41]–[45]. Broadly speaking, these methods are either based on Lagrangian relaxation [41]–[44] or constrained policy optimization [45]. In Lagrangian relaxtion based method, primal and dual variables are updated at different time-scales using gradient ascent/descent. In these methods, constraint satisfaction is guaranteed at convergence. On the other hand, in [45] an algorithm is proposed where constraint satisfaction is enforced in every step throughout training. Our proposed algorithm is based on the PPO algorithm [24], and adopts the Lagrangian relaxation based approach to handle multiple constraints. However, we propose a new method to adapt the Lagrangian penalty multipliers during training, and show that our new approach improves the learning stability of the algorithm. In addition, our work is the first to demonstrate successful policy learning in environments with multiple constraints, and policy transferability among wireless networks of different scales.

C. Background

In this subsection, unconstrained and constrained MDPs are introduced. MDPs and CMDPs are are the classical formalization of sequential decision making and define the interaction between a learning agent and its environment in RL and constrained RL, respectively.

1) Markov Decision Process: An infinite horizon MDP with discounted-returns is defined as a tuple (S, A, P, P_0, R, ζ) , where S and A are finite sets of states and actions, respectively, $\mathcal{P}: \mathcal{S} \times \mathcal{A} \times \mathcal{S} \rightarrow [0,1]$ is the model's state-actionstate transition probabilities, and $\mathcal{P}_0: \mathcal{S} \to [0,1]$ is the initial distribution over the states, $\mathcal{R} : \mathcal{S} \times \mathcal{A} \to \mathbb{R}$, is the immediate reward function which guides the agent through the learning process, and ζ is a discount factor to bound the cumulative rewards and trade-off how far or short sighted the agent is in its decision making. Denote the transition probability from state $s_n = i$ at time step n to state $s_{n+1} = j$ if action $a_n = a$ is chosen by $P_{ij}(a) := P(s_{n+1} = j | s_n = i, a_n = a).$ The transition probability from state i to state j is therefore, $p_{ij} = P(s_{n+1} = j | s_n = i) = \sum_a P_{ij}(a) \pi(a|i)$, where $\pi(a|i)$ is a stochastic policy which maps states to actions. The state-value function of state *i* under policy π is the long-term expected discounted returns starting in state i and following policy π thereafter,

$$V_{\pi}(i) = \sum_{n=1}^{\infty} \sum_{j,a} \zeta^{n-1} P^{\pi}(s_n = j, a_n = a | s_0 = i) \mathcal{R}(j, a),$$

$$\forall i \in \mathcal{S}$$
(1)

Denote the initial distribution over the states by the vector β , where $\beta(i) = P(s_0 = i), \forall i \in S$. The solution of an MDP is a Markov stationary policy π^* that maximizes the inner product $\langle \mathbf{V}_{\pi}, \boldsymbol{\beta} \rangle$,

$$\max_{\pi} \qquad \sum_{n=1}^{\infty} \sum_{j,a} \zeta^{n-1} P^{\pi}(s_n = j, a_n = a) \mathcal{R}(j, a) \qquad (2)$$

There are several approaches to solve (2), including dynamic programming based methods such as value iteration and policy iteration [46], in addition to linear programming based methods [47]. When the model's dynamics, i.e., transition probabilities, are unknown, the Reinforcement Learning (RL) framework can be adopted to find the optimal policies. It is worth to mention that when the agent learns the optimal state-value function and/or the policy as parameterized Deep Neural Networks (DNNs), the agent is commonly referred to as a Deep RL (DRL) agent. There exists a significant body of works with state-of-the-art algorithms to solve the RL problem, which vary by design from value-based methods [48], to policy-based methods [22]–[24], and hybrid actorcritic type algorithms [49]–[53].

2) Constrained Markov Decision Process: In constrained MDPs (CMDPs), additional immediate cost functions $C_k : S \times A \to \mathbb{R}$ are augmented, such that a CMDP is defined by the tuple $(S, A, \mathcal{P}, \mathcal{P}_0, \mathcal{R}, \mathcal{C}, \zeta)$ [35]. The state-value function is defined as in unconstrained MDPs (1). In addition, the infinite-horizon discounted-cost of a state *i* under policy π is defined as,

$$C_{\pi}^{k}(i) = \sum_{n=1}^{\infty} \sum_{j,a} \zeta^{n-1} P^{\pi}(s_{n} = j, a_{n} = a | s_{o} = i) \times C_{k}(j,a), \quad \forall i \in \mathcal{S}, \forall k.$$
(3)

The solution of a CMDP is a markov stationary policy π^* which maximizes $\langle V_{\pi}, \beta \rangle$ subject to the constraints

$$\langle \mathbf{C}_{\pi}^{n}, \boldsymbol{\beta} \rangle \leq E_{k}, \forall k,$$

$$\max_{\pi} \sum_{n=1}^{\infty} \sum_{j,a} \zeta^{n-1} P^{\pi}(s_{n} = j, a_{n} = a) \mathcal{R}(j, a) \qquad (4)$$

$$\sum_{n=1}^{\infty} \sum_{j,a} \zeta^{n-1} P^{\pi}(s_{n} = j, a_{n} = a) \mathcal{C}_{k}(j, a) \leq E_{k}, \forall k$$

$$(4a)$$

Solving for feasible and optimal policies in CMDPs is more challenging compared to unconstrained MDPs, and requires extra mathematical efforts. CMDPs can be solved by defining an appropriate occupation measure and constructing a linear program over this measure, or alternatively by using a Lagrangian relaxation technique in which the CMDP is converted into an equivalent unconstrained problem,

 $\max_{\boldsymbol{\pi}} \min_{\boldsymbol{\eta} \geq 0} \mathcal{L}(\boldsymbol{\pi}, \boldsymbol{\eta})$

(at a)

$$= \max_{\pi} \min_{\eta \ge 0} \langle \mathbf{V}_{\pi}, \boldsymbol{\beta} \rangle - \sum_{k} \eta_{k} \big(\langle \mathbf{C}_{\pi}^{k}, \boldsymbol{\beta} \rangle - E_{k} \big) \quad (5)$$

and invoking the minimax theorem,

$$\max_{\pi} \min_{\eta \ge 0} \mathcal{L}(\pi, \eta) = \min_{\eta \ge 0} \max_{\pi} \mathcal{L}(\pi, \eta)$$
(6)

The right hand side of (6) can be solved on two-time scales: on a faster time scale gradient-ascent is performed on state-values to find the optimal policy for a given set of Lagrangian variables, and on a slower time scale, gradientdescent is performed on the dual variables [35]. Past works explore this primal-dual optimization approach for CMDPs with known model dynamics and tabular-based RL methods with unknown model dynamics [36]-[40]. In the realm of deep RL where policies and value functions are parameterized neural networks, recent works which apply primal-dual optimization for generic benchmark problems are emerging [41]–[45]. None of these works, however, apply primal-dual optimization techniques in the wireless networking domain. Furthermore, practical wireless networking systems admit multiple constraints, which can be conflicting. This incurs extra difficulty for policy search and optimization, and may cause learning instability. Our proposed approach tackles these issues and demonstrates successful policy learning in wireless environments with multiple constraints.

III. SYSTEM MODEL

Consider a multi-UAV based IoT network consisting of M UAVs and N IoT devices, where the UAVs collect data from a massive deployment of IoT devices, as shown in Figure 1(a). Let $\mathcal{M} = \{1, \dots, M\}$ be the set of UAVs, and $\mathcal{N} = \{1, \dots, N\}$ be the set of IoT devices. UAVs are connected via wireless back-haul links to a central controller, which controls the altitude of each UAV and manages the access parameters of wireless IoT devices. IoT devices are independently and uniformly distributed (i.u.d.) across a deployment area \mathbb{A} . Let the locations of IoT devices be $\{\hat{x}^i, \hat{y}^i\}_{i=1}^N$. Each IoT device is served by the closest UAV. Denote the subset of IoT devices which are associated with UAV m by $\mathcal{N}_m \subset \mathcal{N}$,

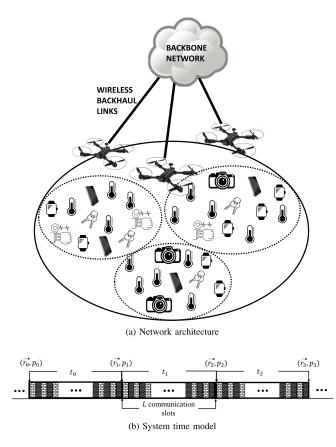


Fig. 1. Multi-cell UAV based wireless IoT network.

 $|\mathcal{N}_m| \leq N, \bigcup_{m=1}^M \mathcal{N}_m = \mathcal{N}, \mathcal{N}_i \cap \mathcal{N}_j = \phi, \forall i \neq j \in \mathcal{M}.$ Time is slotted into fixed-length discrete time units indexed by n. For instance, the n-th time slot is $[t_n, t_{n+1})$, where $t_{n+1} - t_n = \Delta t$, $\forall n$. Each time slot n is further divided into L communication sub-slots of length $\frac{\Delta t}{L}$ each, as shown in 1(b). Denote the l-th communication sub-slot in slot n by $t_n^l, l = \{0, \dots, L-1\}$. During these communication sub-slots, IoT devices contend for channel access based on an adaptive ppersistent slotted Aloha MAC protocol. In this protocol, an IoT device waits until the beginning of a communication sub-slot before attempting to access the channel with probability p, which is adapted every time slot by the central controller based on network dynamics¹. IoT devices transmit uplink data to their associated UAV with a fixed transmission power of P_{TX} watts, and are traffic-saturated, i.e., there is always a data packet ready for transmission.

Denote the location of UAV m during time slot n by $r_m(t_n) = (x^m, y^m, z_n^m)$. In our system model, z_n^m is dynamically adjusted by the central controller, while the the planar location of the UAVs, $(x^m, y^m), \forall m \in \mathcal{M}$ are determined a priori by using Lloyd's K-means clustering algorithm to partition the distribution of IoT devices on the ground into K = M Voronoi cells, such that the sum of squared distances between any IoT device and its nearest UAV is

minimized [54]². Let $u_n^{i,m} = \{0,1\}$ indicate whether IoT device *i* is associated with UAV *m* during time slot *n*. If UAV *m* located at $r_m(t_n)$ during the *n*-th time slot is the closest to IoT device *i*, $u_n^{i,m} = 1$, and $u_n^{i,l} = 0, \forall l \neq m$. The power of the signal transmitted by a wireless IoT device *i* to a UAV *m* is subject to independent Rayleigh channel fading, $h_{i,m}(t_n)^3$, and a distance-dependent free-space path-loss $d_{i,m}^{-\alpha}(t_n)$, where α is the path-loss exponent, and $d_{i,m}^{-\alpha}(t_n)$ is the propagation distance between IoT device *i* and UAV *m*, $d_{i,m}(t_n) = \sqrt{(x^m - \hat{x}^i)^2 + (y^m - \hat{y}^i)^2 + (z_n^m)^2}$. The received power at UAV *m* from IoT device *i* in a communication sub-slot t_n^l is,

$$P_{RX}^{i,m}(t_n^l) = \begin{cases} \hat{\mathcal{I}}_i(t_n^l)c_0 \ h_{i,m}(t_n)P_{TX}d_0^{-\alpha}, & d_{i,m}(t_n) \le d_0, \\ \hat{\mathcal{I}}_i(t_n^l)c_0 \ h_{i,m}(t_n)P_{TX}d_{i,m}^{-\alpha}(t_n), & d_{i,m}(t_n) \ge d_0, \end{cases}$$
(7)

where $c_0 = \frac{\lambda^{\alpha}}{(4\pi)^{\alpha}}$ is a constant which depends on the wavelength of the transmitted signal, λ , and d_0 is a reference distance. $\hat{\mathcal{I}}_i(t_n^l)$ is a Bernoulli random variable with parameter $p(t_n) \in (0, 1]$ which indicates whether IoT device *i* transmits during communication sub-slot t_n^l , i.e., $\hat{\mathcal{I}}_i(t_n^l) = 1$ with probability $p(t_n)$. UAV *m* first decodes the signal with the highest signal power under the interference from all other IoT devices involved in the NOMA transmissions. Without loss of generality, IoT devices $\mathcal{I}_m(t_n^l) = \{i | \hat{\mathcal{I}}_i(t_n^l) = 1\}$ are sorted in the descending order of their received signal strength at UAV *m*, such that i = 1 is the IoT device with the highest received signal to interference plus noise (SNIR) at UAV *m*, and i = 2 is the IoT device with the second highest received SNIR at UAV *m*⁴. The highest received SNIR at UAV *m* in a communication sub-slot t_n^l is therefore,

$$\text{SNIR}_{1,m}(t_n^l) = \frac{P_{RX}^{1,m}(t_n^l)}{n_0 + \sum_{k \in \mathcal{I}_m(t_n^l) \setminus 1} P_{RX}^{k,m}(t_n^l)}, \qquad (8)$$

where n_0 is the noise floor power. Similarly, the second highest received SNIR at UAV m in a communication sub-slot t_n^l is,

$$\text{SNIR}_{2,m}(t_n^l) = \frac{P_{RX}^{2,m}(t_n^l)}{n_0 + \sum_{k \in \mathcal{I}_m(t_n^l) \setminus \{1,2\}} P_{RX}^{k,m}(t_n^l)}, \quad (9)$$

UAV m can decode the signal with $SNIR_{1,m}(t_n^l)$ if

- 1) user 1 is associated with UAV m during communication sub-slot n, $u_n^{1,m} = 1$, and,
- 2) $\text{SNIR}_{1,m}(t_n^l)$ is larger than the SNIR threshold, i.e., $U(\text{SNIR}_{1,m}(t_n^l)) = \text{SNIR}_{1,m}(t_n^l)$,

²Lloyd's K-means clustering algorithm is an iterative algorithm to determine a set of K centroids given a large set of IoT device locations $\{\hat{x}^i, \hat{y}^i\}_{i=1}^N$, so as to minimize the within-cluster variance (sum of squared distances to cluster centroid), $\min_{\{(x^m, y^m)\}} \sum_{m=1}^M \sum_{i \in \mathcal{N}_m} ||(\hat{x}^i, \hat{y}^i) - (x^m, y^m)||^2$. Given that the range of vertical flight is the dominant factor in our system model, determining the planar locations of UAVs a priori reduces the number of control variables without adversely impacting network performance, as will be shown in Sec. V.

³The statistical channel state information, $h_{i,m}(t_n)$, is assumed to be quasistatic and is fixed during a time slot n.

⁴We consider the two highest received signals to trade-off NOMA gain and SIC decoding complexity for uplink transmissions.

¹Implementing time-synchronization among IoT devices is important to enable NOMA decoders. Without time-synchronization, transmissions may partially overlap which makes the design of NOMA decoders hard.

where U(.) is a thresholding function to maintain a minimum quality of service,

$$U(\text{SNIR}_{i,m}(t_n^l)) = \begin{cases} 0, & \text{SNIR}_{i,m}(t_n^l) < \text{SNIR}_{\text{Th}}, \\ \text{SNIR}_{i,m}(t_n^l), & \text{SNIR}_{i,m}(t_n^l) \ge \text{SNIR}_{\text{Th}}. \end{cases}$$
(10)

In addition, UAV m can decode the signal with $SNIR_{2,m}(t_n^l)$ if

- 1) The signal with $SNIR_{1,m}(t_n^l)$ is successfully decoded,
- 2) user 2 is associated with UAV m during communication sub-slot n, $u_n^{2,m} = 1$, and, 3) SNIR_{2,m} (t_n^l) is larger than the SNIR threshold,
- i.e., $U(\text{SNIR}_{2,m}(t_n^l)) = \text{SNIR}_{2,m}(t_n^l)$

The sum rates of the received data at UAV m in communication sub-slot t_n^l is,

$$G_m(t_n^l) = \mathcal{W} \log_2 \left(1 + U(\operatorname{SNIR}_{1,m}(t_n^l)) u_n^{1,m} \right) + \mathcal{W} \log_2 \left(1 + U(\operatorname{SNIR}_{2,m}(t_n^l)) u_n^{1,m} u_n^{2,m} e_n^{1,m} \right)$$
(11)

where \mathcal{W} is the transmission bandwidth, and $e_n^{1,m} = 1$ if $U(\text{SNIR}_{1,m}(t_n^l)) = \text{SNIR}_{1,m}(t_n^l)$ and 0 otherwise. The total network capacity in any given system slot t_n ,

$$\mathbb{G}(t_n) = \sum_{l=0}^{L-1} \sum_{m \in \mathcal{M}} G_m(t_n^l)$$
(12)

On the other hand, UAVs are equipped with solar panels, which harvest solar energy to replenish the on-board battery. The attenuation of solar light passing through a cloud can be modeled based on [32],

$$\phi(d^{cloud}) = e^{-\beta_c d^{cloud}} \tag{13}$$

where $\beta_c \ge 0$ denotes the absorption coefficient of the cloud, and d^{cloud} is the distance that the solar light travels through the cloud. Following [32] and the references therein, the solar energy harvested by UAV m during time slot n can be modeled as,

$$E_{\rm H}^{m}(t_{n}) = \begin{cases} \psi \tilde{S}\tilde{G}\Delta t, \\ \frac{z_{n}^{m} + z_{n+1}^{m}}{2} \ge z_{high} \\ \psi \tilde{S}\tilde{G}\phi(z_{high} - \frac{z_{n}^{m} + z_{n+1}^{m}}{2})\Delta t, \\ z_{low} \le \frac{z_{n}^{m} + z_{n+1}^{m2}}{2} < z_{high} \\ \psi \tilde{S}\tilde{G}\phi(z_{high} - z_{low})\Delta t, \\ \frac{z_{n}^{m} + z_{n+1}^{M}}{2} < z_{low} \end{cases}$$
(14)

where ψ is a constant representing the energy harvesting efficiency, \hat{S} is the area of solar panels, and \hat{G} denotes the average solar radiation intensity on earth. z_{high} and z_{low} are the altitudes of upper and lower boundaries of the cloud. During time-slot n, UAV m can cruise upwards or downwards from $r_m(t_n)$ to $r_m(t_{n+1})$. The energy consumed by UAV m during time slot n [32] is,

$$E_{\rm C}^m(t_n) = \left(\frac{W^2/(\sqrt{2}\rho A)}{4^{0.25}V_z} + Wv_z + P_{\rm static} + P_{\rm antenna}\right)\Delta t,$$
$$v_z = \frac{z_{n+1}^m - z_n^m}{\Delta t} \tag{15}$$

where, $V_z = \sqrt{\frac{W}{2\rho A}}$, W is the weight of the UAV, ρ is air density, and A' is the total area of UAV rotor disks. P_{static} is the power consumed for maintaining the operation of UAV, and P_{antenna} is the power consumed by the receiving antenna. It is worth to mention that cruising upwards consumes more power than cruising downward and hovering.

Denote the battery energy storage of UAV m at the beginning of slot n by $B_m(t_n)$. The battery energy in the next slot is given by,

$$B_m(t_{n+1}) = \min\{[B_m(t_n) + E_{\rm H}(t_n) - E_{\rm C}^m(t_n) + \mathbb{B}(t_n)]^+, B_{\rm max}\},$$
(16)

where $\mathbb{B}(t_n), \forall n$, are independent zero-mean gaussian random variables with variance σ_B^2 which characterizes the randomness in the battery evolution process, and $[]^+$ denotes the positive part.

IV. PROBLEM FORMULATION AND PROPOSED CDRL ALGORITHM

In order to maximize the total network capacity under stochastic mutual interference of IoT devices while ensuring energy sustainability of UAVs over the operating horizon H, the central controller decides on the altitude of each UAV $m, \forall m \in \mathcal{M}$, at the beginning of each slot n, z_n^m , as well as the channel access probability $p(t_n)$ of IoT devices considering the potential access gain provisioned by NOMA. The channel access probability will be broadcast to IoT devices through beacons at the beginning of each time slot, so that IoT devices adapt their random channel access parameter and maintain slotted-time synchronization.

The problem of maximizing the total network capacity while ensuring energy sustainability of each UAV is a constrained stochastic optimization problem over the operating horizon due to random channel access, the stochastic channel model, dynamic network topology, and the stochastic energy evolution in the batteries of UAVs. Moreover, this problem is mathematically intractable because of the combinatorial space of possible transmissions and channel interference events induced by the random access protocol, and hence offline solutions cannot be devised. To solve this problem and find an energysustainable capacity-optimal control policy, we formulate it as a CMDP and design an online Constrained Deep Reinforcement Learning (CDRL) algorithm by combining state-ofthe-art DRL policy optimization algorithms with Lagrangian primal-dual techniques.

A. CMDP Formulation

To enable continuous control of UAVs altitudes and channel access probability, we consider parametrized DNN based policies with parameters θ , and parametrized state-value function with parameters Θ henceforth. We formulate the joint problem of UAVs altitude control and random channel access of IoT devices as a discrete-time CMDP with continuous state and action spaces as follows,

$$1) \forall s_n \in \mathcal{S},$$

$$s_n = \bigcup_{\mathcal{M}} \left\{ z_n^m, \cdots, z_{n-h_k}^m, B_m(t_n), \cdots, B_m(t_{n-h_k}), P(\text{SNIR}_{1,m}(t_n^l) \ge \text{SNIR}_{\text{Th}}), P(\text{SNIR}_{2,m}(t_n^l) \ge \text{SNIR}_{\text{Th}}), \\ \mathbb{E}[\text{SNIR}_{1,m}(t_n^l)|\text{SNIR}_{1,m}(t_n^l) \ge \text{SNIR}_{\text{Th}}], \\ \mathbb{E}[\text{SNIR}_{2,m}(t_n^l)|\text{SNIR}_{2,m}(t_n^l) \ge \text{SNIR}_{\text{Th}}], \\ \text{Var}[\text{SNIR}_{1,m}(t_n^l)|\text{SNIR}_{1,m}(t_n^l) \ge \text{SNIR}_{\text{Th}}], \\ \text{Var}[\text{SNIR}_{2,m}(t_n^l)|\text{SNIR}_{2,m}(t_n^l) \ge \text{SNIR}_{\text{Th}}], \\ \text{Var}[\text{SNIR}_{2,m}(t_n^l)|\text{SNIR}_{2,m}(t_n^l) \ge \text{SNIR}_{\text{Th}}], \\ \end{bmatrix}$$

i.e., the state space encompasses $\forall m$, the current altitude of UAV m along with h_k historical altitudes, current battery energy of UAV m along with h_k historical battery energies, probability the highest and second highest received SNIRs from associated users at UAV m is greater than or equal to SNIR_{Th}, the mean of the highest and second highest received SNIRs from associated users at UAV m given that they are greater than or equal to the SNIR threshold, and the variance of the highest and second highest received SNIRs from associated users at UAV m given that they are greater than or equal to the SNIR threshold. Here, the mean and variance are calculated over the L communication sub-slots.

- ∀a_n ∈ A, a_n = ⋃_M {Δz_n^m} ∪ {p(t_{n+1})}, where Δz_n^m = z_{n+1}^m − z_n^m, i.e., the action space encompasses the altitude displacement of each UAV between any two consecutive time slots, and the random channel access probability in the next system slot.
- 3) $\mathcal{R}(s_n, a_n) = \frac{\mathbb{G}(t_n)}{H}$, i.e., the immediate reward at the end of each time slot n is the total network capacity during slot n, normalized by the operating horizon H.
- slot n, normalized by the operating horizon H.
 4) C_m(s_n, a_n) = B_m(t_n)-B_m(t_{n+1})/B_{max}, ∀m, i.e., the immediate cost at the end of each slot n is the change in the battery energy between any two consecutive time slots, which is caused by the displacement of each UAV m, normalized by the maximum battery energy.
- 5) $E_m = -B_{min}/B_{max}$, $\forall m$, i.e., the upper bound on the long-term expected cost is the normalized negative of the minimum desired battery energy increase at the end of the planning horizon over the initial battery energy.

Based on this formulation, the objective is to find a Markov policy $\pi_{\theta_{\pi}}$ which maximizes the long-term expected

discounted total network capacity, while ensuring energy sustainability of each UAV m over an operating horizon,

$$\max_{\boldsymbol{\theta}_{\pi}} \mathbb{E}_{\pi_{\boldsymbol{\theta}}}^{\beta} \Big[\sum_{n=0}^{\infty} \zeta^{n} \mathbb{G}(t_{n}) \Big] \\ \mathbb{E}_{\pi_{\boldsymbol{\theta}}}^{\beta} \Big[\sum_{n=0}^{H} B_{m}(t_{n}) - B_{m}(t_{n+1}) \Big] \leq -B_{min}, \quad \forall m \quad (17)$$

Problem (17) exhibits trade-offs between total system capacity and energy sustainability of UAVs. For instance, a UAV hovering at a higher altitude above the cloud cover can harvest more solar energy to replenish its on-board battery storage, as given by (14). However, at higher altitudes, the received signal power at a UAV from IoT devices will be smaller due to the log-distance path loss model, and consequently, the system capacity will be smaller. The converse is true, that is, when a UAV hovers at lower altitudes, network capacity is improved, yet solar energy harvesting is heavily attenuated. In addition, based on the network topology at any time slot n, spatial gain and NOMA overload vary. An optimal stochastic control policy for altitude control of UAVs and channel access management of IoT devices should be therefore learned online. In the following subsection, we propose an online CDRL algorithm to solve (17).

B. Proposed CDRL Algorithm

To solve (17) in absence of the state-action-state transition probabilities of the Markov model, we adopt the RL framework in which an autonomous agent learns an optimal policy by repeated interactions with the wireless environment [46]. The wireless environment provides the agent with rewards and costs signals, which the agents exploit to further improve its policy. Our proposed algorithm is based on the state-of-theart Proximal Policy Optimization (PPO) algorithm [24], and leverages the technique of primal-dual optimization [42]. The architecture of our proposed algorithm is shown in Figure 2.

In the proposed CDRL algorithm, parameterized DNN of the policy $\pi_{\theta}(a|s)$ is learned by maximizing the PPO-clip objective function, which is a specially designed clipped surrogate advantage objective that ensures constructive policy updates,

$$O^{\mathsf{clip}}(\boldsymbol{\theta}) = \hat{\mathbb{E}}_{n} \Big[\min\Big(\frac{\pi_{\boldsymbol{\theta}}(a_{n}|s_{n})}{\pi_{\boldsymbol{\theta}_{\mathsf{old}}}(a_{n}|s_{n})} \hat{A}_{n}, \mathsf{clip}(\frac{\pi_{\boldsymbol{\theta}}(a_{n}|s_{n})}{\pi_{\boldsymbol{\theta}_{\mathsf{old}}}(a_{n}|s_{n})}, 1+\epsilon, 1-\epsilon) \hat{A}_{n} \Big) \Big],$$
(18)

where θ are the policy neural network parameters, ϵ is a clip fraction, and \hat{A}_n is the generalized advantage estimator (GAE) [55]⁵,

$$\hat{A}_{n} = \sum_{l=0}^{\infty} (\zeta\xi)^{l} \big(\hat{\mathcal{R}}_{n+l} + \zeta V_{\Theta}(s_{n+l+1}) - V_{\Theta}(s_{n+l}) \big).$$
(19)

Clipping in (18) acts as a regularizer which controls how much the new policy can go away from the old one while still

⁵The advantage function is defined as the difference between the stateaction value function and the value function, $A(s_n, a_n) = Q(s_n, a_n) - V(s_n)$. GAE makes a compromise between bias and variance in estimating the advantage.

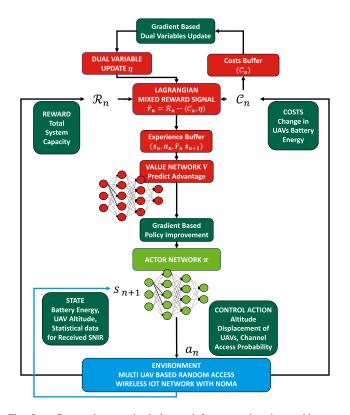


Fig. 2. Proposed constrained deep reinforcement learning architecture. Constrained policy optimization is performed on three time scales. On the fastest time scale, the state-value function is updated by minimizing (22), then the policy is updated by maximizing (18) on the intermediate time-scale, and finally, the Lagrangian multipliers are updated on the slowest time-scale by minimizing (21).

improving the training objective. In order to further ensure reasonable policy updates, we adopt a simple early stopping method in which gradient optimization on (18) is terminated when the mean KL-divergence between the new and old policy reaches a predefined threshold KL_{Th}. In (19), $\hat{\mathcal{R}}_n = \hat{\mathcal{R}}_n(s_n, a_n, \eta)$ is a Lagrangian penalized reward signal [41],

$$\hat{\mathcal{R}}(s_n, a_n, \boldsymbol{\eta}) = \mathcal{R}(s_n, a_n) - \sum_m \eta_m \mathcal{C}_m(s_n, a_n).$$
(20)

In our proposed algorithm, the Lagrangian penalty multipliers are updated adaptively according to policy feasibility by performing gradient descent on the original constraints. Given that η are initially set to 0, i.e., the agent is initially indifferent to the cost constraints, we propose to learn the Lagrangian penalty multipliers by minimizing the following loss function with respect to η in order to ensure learning stability and convergence to a local saddle point,

$$O^{P}(\boldsymbol{\eta}) = \frac{1}{B_{max}} \sum_{m} \eta_{m} \operatorname{clip} \left(-B_{min} - \mathbb{E}_{\pi_{\boldsymbol{\theta}}}^{\beta} \left[\sum_{n=0}^{H} B_{m}(t_{n}) - B_{m}(t_{n+1}) \right], -\infty, 0 \right)$$
(21)

If a constraint *m* is violated, then $\frac{\partial O^P}{\partial \eta_m} < 0$, and so η_m will be increased to enforce the constraint. Due to clipping, η_m will not be updated if the constraint *m* is satisfied. By ensuring that η are monotonously increased starting from $\eta_0 = 0$ during

training, the agent avoids oscillations between the feasible and infeasible policy spaces when optimizing the policy parameters (18), which improves learning stability.

Finally, the state-value function is learned by minimizing the mean squared error loss against the policy's discounted rewards-to-go,

$$O^{\mathsf{V}}(\mathbf{\Theta}) = \hat{\mathbb{E}}_n \Big[\Big(V_{\mathbf{\Theta}}(s_n) - \sum_{l=0}^{\infty} \zeta^l \hat{\mathcal{R}}_{n+l}(s_{n+l}, a_{n+l}) \Big)^2 \Big].$$
(22)

The optimization in our proposed algorithm is performed over three time-scales, on the fastest time scale, the state-value function is updated by minimizing (22), then the policy is updated by maximizing (18) on the intermediate time-scale, and finally, the Lagrangian multipliers are updated on the slowest time-scale by minimizing (21). Optimization timescales are controlled by choosing the maximum learning rate of the stochastic gradient optimizer used, e.g., adaptive moment estimation (ADAM) [56], as well as the number of gradient steps performed at the end of each training epoch. The full algorithmic procedure for training the CDRL agent is outlined in Algorithm 1.

Algorithm 1 Constrained PPO-Clip					
Input : Initial policy network parameters θ , initial value					
network parameters Θ , initial Lagrange					
multipliers $\eta = 0$					
for $epoch = 0, 1, \cdots$ do					
for $n = 0, 1, \dots, H$ do					
Observe initial state s_n					
Sample action $a_n \sim \pi_{\theta}(a_n s_n)$					
Take action a_n					
Receive reward $\mathcal{R}(s_n, a_n)$, M costs $\mathcal{C}_m(s_n, a_n)$,					
and new state s_{n+1}					
Compute penalized reward $\hat{\mathcal{R}}(s_n, a_n, \eta)$ using (20)					
Store transition $(s_n, a_n, \hat{\mathcal{R}}(s_n, a_n, \eta), s_{n+1})$ in					
policy training buffer					
Store $\mathcal{C}_{k,\forall k}(s_n, a_n)$ in Lagrange multiplier training					
buffer					
end					
Compute rewards to go					
Compute advantage estimate \hat{A}_n using GAE (19) and					
current value network					
for $k = 0, 1, \cdots$ do					
Update policy parameters θ_k via stochastic					
gradient ascent with ADAM on the PPO-Clip					
objective (18)					
Compute KL-divergence between new policy and					
old policy					
Break if KL-divergence hits KL _{Th}					
end					
for $k = 0, 1, \cdots$ do					
Fit the value network via stochastic gradient descent with ADAM on (22)					
end					
Update Lagrangian multipliers via stochastic gradient					
descent with ADAM on (21)					
end					

To parameterize the space of continuous control policies, a parameterized stochastic Gaussian policy is adopted [46],

$$\pi_{\boldsymbol{\theta}}(a_n|s_n) = \frac{1}{\sigma(s_n, \boldsymbol{\theta}_{\boldsymbol{\sigma}})\sqrt{2\pi}} \exp\Big(-\frac{(a_n - \mu(s_n, \boldsymbol{\theta}_{\boldsymbol{\mu}}))^2}{2\sigma(s_n, \boldsymbol{\theta}_{\boldsymbol{\sigma}})^2}\Big).$$
(23)

where θ_{μ} are the DNN parameters for the mean of the policy, and θ_{σ} are the DNN parameters for the variance of the policy. The choice of a gaussian policy is commonly adopted in DRL because the gradient of the policy as well as the log probabilities necessary for KL-divergence computation can be derived in a closed form [46]. At the beginning of training, the variance of the policy network encourages exploration. As training progresses, the variance of the policy is reduced due to maximizing (18) and in doing so, the policy shifts slowly towards the deterministic policy given by $\mu(s_n, \theta_{\mu})$.

CDRL Implementation and Training: A fully connected multi-layer perceptron network with three hidden layers for both the policy and value networks are used. Each hidden layer has 128 neurons. Tanh activation units are used in all neurons. The range of output neurons responsible for the altitude displacement of each UAV is linearly scaled to $[\Delta z_{min}, \Delta z_{max}]$ so as to limit the maximum cruising velocity of the UAVs. The range of the output neuron controlling the random channel access probability is linearly scaled to $[0, \frac{2}{N}]$. The weights of the policy network are heuristically initialized to generate a feasible policy. The variance of the Gaussian policy is state-independent, $\sigma(s_n, \theta_{\sigma}) = \theta_{\sigma}$, with initial value $\theta_{\sigma}^0 = e^{-0.5}$.

Training of the proposed CDRL agent has been performed over 1000 epochs, where each epoch corresponds to 32 episodes, and each episode corresponds to trajectories of length H = 360 time steps, amounting for about 11.5 million training samples. At the end of each episode, the trajectory is cut-off and the wireless system is reinitialized. Episodes in each epoch are rolled-out in parallel by 32 Message Passing Interface (MPI) ranks, to sample 32 trajectories and reduce gradient estimation variance. After each MPI rank completes its episodic roll-out, Lagrangian primal-dual policy optimization is performed as outlined in Algorithm 1 based on the average gradients of the MPI ranks, such that the DNN parameters θ , Θ , and the Lagrange multipliers η , remain synchronized among the 32 MPI ranks during training. At the end of training, the trained policy network corresponding to the mean of the learned Gaussian policy, $\mu(s_n, \theta_\mu)$, is used to test its performance through the simulated environment.

V. PERFORMANCE EVALUATION

We have developed a simulator in Python for the solarpowered multi-UAV based Wireless IoT network with NOMA described in section III, and implemented the proposed CDRL algorithm based on OpenAI's implementation of PPO [57]. We trained the proposed CDRL agent in a multi-cell wireless IoT network of M = 2 solar-powered UAVs and N =200 IoT devices. At testing, N is varied to demonstrate the efficacy of the trained CDRL in managing massive number of IoT devices. IoT devices were deployed independently

TABLE I Simulation Parameters

Parameter	Value	Parameter	Value		
P_{TX}	$30 \ dBm$	B_{min}	22 Wh		
α	2		0.4		
Δt	10s	$\psi \\ ilde{S} \\ ilde{G}$	$1m^2$		
f_0	900 MHz	\tilde{G}	$1367W/m^{2}$		
d_0	1m	W	$39.2kg * m/s^2$		
$h_{i,m}$	exp(1)	ρ	$1.225 kg/m^{3}$		
n_0	-80 dBm	A	$0.18m^{2}$		
\mathcal{W}	1Hz	$P_{static} + P_{antenna}$	5 watts		
SNIR _{Th}	10dB	ϵ	0.2		
L	1000	h_k	4		
β_c	0.01	H	360 (1hr)		
z_{high}, z_{low}	$1.3, 0.7 { m km}$	$\Delta z_{min}, \Delta z_{max}$	-40m, 40m		
z_{min}, z_{max}		ξ	0.97		
B_{max}	222 Wh	$\eta_{ m lr}$	3×10^{-3}		
ζ	0.999	$\Theta_{ m lr}$	10^{-3}		
KL_{Th}	0.01	$\theta_{ m lr}$	3×10^{-4}		
σ_B^2	500				
_ 1000	-				
D 900					
jero					
표 600	-				
S 400					
008 (J) 009 Mean Solar Energy 005 008 (J)					

600 800 1000 1200 1400 Altitude (m)

Fig. 3. Solar energy output of solar panels versus UAV altitude. Solar energy decays exponentially through the cloud cover between 1300m and 700m.

and uniformly within a grid of $[0,0] \times [1500, 500]$ m. The two UAVs were initially deployed at (250, 250, 750)m and (750, 250, 1250)m with 50% initial battery energy, i.e., 111 Wh. Notice that the x and y coordinates of the two UAVs, i.e., (250, 250)m and (750, 250)m, are minimizers of the sum of squared planar distances between IoT devices and the closest UAV, as determined by Lloyd's K-means clustering algorithm for the uniform random deployment of IoT devices on the ground. The impacts of different planar UAV deployments on network performance will also be investigated. UAVs were allowed to cruise vertically between 500m and 1500m. The main simulation parameters for the experiments are outlined in Table I. UAV related parameters are based on the work of [32].

The output energy of solar panels mounted on the UAV as a function of altitude according to (14) is shown in Figure 3. The highest solar energy is achieved when the UAV is above the cloud cover at $z_{high} = 1300$ m. Notice how solar energy decays exponentially through the clouds which extend down to $z_{low} = 700$ m. When the UAV is below 700m, the output energy of its solar panels is zero. UAVs cruising above 1300m harvest the most solar energy, while UAVs cruising below 700m harvest the least energy. Hovering at low altitudes reduces distance-dependant path-loss and improves the wireless channel capacity, however, it is not energy sustainable.

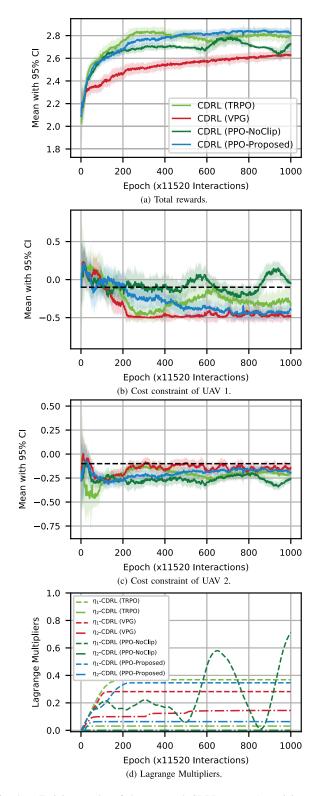


Fig. 4. Training results of the proposed CDRL agent. As training progresses, the proposed CDRL agent becomes more experienced; collects higher expected total rewards, and better satisfies the energy constraints. Proposed CDRL agent outperforms other agents and possesses an improved learning stability thanks to clipping in (18) and (21).

The learning curves of the trained CDRL agent, (PPO-Proposed), are shown in Figure 4. To evaluate the effects of policy optimization in our proposed CDRL framework, we have compared the learning performance with two other

DRL agents which adopt different policy optimization algorithms, namely, (TRPO) [22] and (VPG) [23]. In these algorithms, the Lagrangian penalty multipliers are adapted during training as in Algorithm 1 by minimizing (21) with respect to η . In addition, we demonstrate the effects of clipping in (21) on learning stability by training a CDRL agent (PPO-NoClip), which adopts PPO for policy optimization, yet it adapts the Lagrange penalty multipliers by minimizing an unclipped version of (21) with respect to η . It can be seen from Figure 4(a) that the CDRL agent becomes more experienced as training progresses and collects higher expected total rewards. In addition, the proposed CDRL agent becomes more experienced in satisfying energy constraints as can be seen from Figures 4(b)-(c), and learns a policy whose expected costs fall below the normalized energy constraint upper bound $-B_{min}/B_{max} = -0.1$. The proposed CDRL agent outperforms both CDRL (TRPO) and CDRL (VPG) in terms of the achieved total rewards during training. Compared with CDRL (TRPO) and CDRL (VPG), the proposed CDRL agent also exhibits a relatively more stable constraint satisfaction during training. This finding is consistent with previous works which demonstrates the superiority of PPO as a policy optimization algorithm on a variety of benchmark tasks [24]. On the other hand, the convergence of the Lagrangian multipliers to non-negative values during the training of the proposed CDRL algorithm is shown in Figure 4(d). It can be observed that the two cost constraints are penalized differently, which is primarily due to the different initial conditions and different terminal states. The Lagrangian multiplier of the energy constraint corresponding to UAV 1 is larger than that of UAV 2, therefore it is expected that UAV 1 will end up its flight with more harvested energy in its battery. Notice that in the case of (PPO-NoClip), where the Lagrange penalty multipliers are adapted during training by minimizing an unclipped version of (21), the Lagrange multipliers fluctuate which leads to oscillations between the feasible and infeasible policy spaces as can be seen from Figure 4(b). On the other hand, agents in which the Lagrangian penalty multipliers are adapted by minimizing the clipped objective (21), have monotonously increasing Lagrange multipliers which converge early during training. Clipping in (21) results in a better learning stability and constraint satisfaction compared with (PPO-NoClip), as can be seen from Figures 4(a)-(c).

The learned policy by our proposed CDRL algorithm is shown in Figure 5. It can be seen from Figures 5(a) and 5(b) that the CDRL agent learns a policy in which the two UAVs take turns in cruising upwards to recharge their on-board batteries, and in serving IoT devices deployed on the ground. UAV 2 first climbs up to recharge its battery, while UAV 1 descends down to improve communication performance for IoT devices on the ground. Since IoT devices are associated with the closest UAV, in this case, all IoT devices are associated with UAV 1. When UAV 2's battery is fully charged, it descends down gradually to switch roles with UAV 1: UAV 2 becomes the BS with which all IoT devices are associated, while UAV 1 climbs up to recharge its battery. Such a policy ensures that the battery energy of the two UAVs is not drained throughout the operating horizon as can

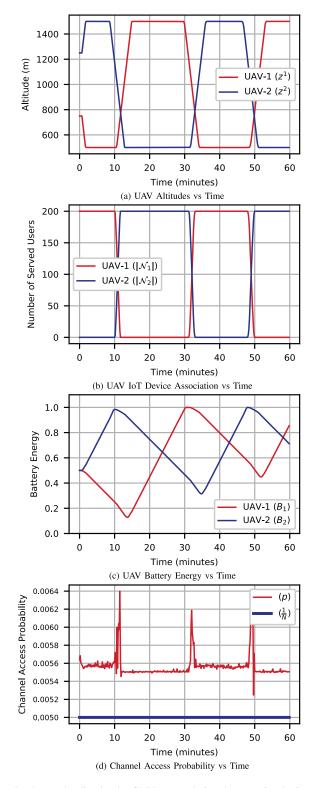


Fig. 5. Learned policy by the CDRL agent during the operating horizon of the two UAVs. A cooperative policy among UAVs is learned in which the two UAVs take turns to recharge the battery and provision uninterrupted wireless service to IoT devices.

be seen from Figure 5(c). Note that the terminal energy in UAV's 1 battery is higher than that of UAV 2, which is expected based on the observation that the Lagrange multiplier corresponding to UAV's 1 energy constraint is larger than that of UAV 2. In Figure 5(d), the random channel access

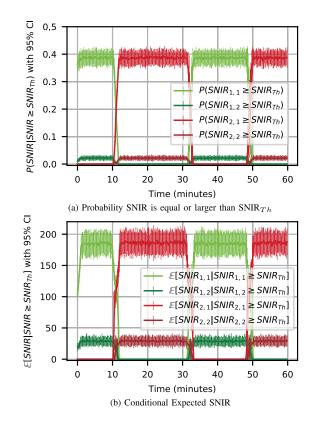


Fig. 6. NOMA performance based on the learned CDRL policy during the operating horizon of the two UAVs. NOMA's gain is higher in steady states when all IoT devices are associated with the same UAV, compared to transient states when the two UAVs exchange roles and are both serving IoT devices.

probability based on the learned CDRL policy is shown. It can be observed that when either of the two UAVs is fully serving all the 200 IoT devices, the wireless networking system is overloaded with p > 1/N, thanks to spatial gain and NOMA. Note that p = 1/N is the optimal transmission probability in single-cell p-persistent slotted Aloha systems, which is oblivious to NOMA and the heterogeneous channel conditions of IoT devices. The channel access probability is dynamically adapted when the two UAVs cruise upward and downward to exchange roles in the wireless system. At times when both UAVs have associated users, the channel access probability can be seen to spike higher to maintain NOMA overload, as can be observed from Figures 6(a)-(b). It can be seen from these two figures that NOMA's gain is higher in steady states when all IoT devices are associated with the same UAV, compared to transient states when the two UAVs exchange roles and are both serving IoT devices. This is because it is less likely that the second highest received SINR to a UAV is from within the same cell at times when both UAVs provision wireless service. By deploying multiple UAVs, it is therefore possible to learn a cooperative policy in which UAVs take turns to charge their battery and provision uninterrupted wireless service.

To evaluate the efficacy of the learned policy, we have compared its performance with three baseline policies which are learned by 1) an unconstrained PPO agent which is energy-unaware (RL Energy-Unaware), i.e., the agent attempts to maximize the wireless network capacity with indifference to battery energy dissipation of the UAVs, 2) an

 TABLE II

 Performance Comparison With Baseline Algorithms

	RLWS	RLWS	RLWS	Random	Proposed
	$\eta_1 = 0, \eta_2 = 0$	$\eta_1 = 0, \eta_2 = 10$	$\eta_1 = 10, \eta_2 = 10$	Policy	CDRL
$(\min_n z_1(t_n), \mathcal{G}_n[z_1(t_n)], \max_n z_1(t_n)), m$	500, 504, 750	500, 509, 750	750, 1462, 1500	500, 803, 1500	500, 865, 1500
$(\min_n z_2(t_n), \mathcal{G}_n[z_2(t_n)], \max_n z_2(t_n)), m$	500, 520, 1250	1250, 1489, 1500	1250, 1494, 1500	500, 1053, 1500	500, 815, 1500
$(\min_n B_1(t_n), \mathcal{G}_n[B_1(t_n)], \max_n B_1(t_n)), \%$	0.0, 0.0, 0.5	0.0, 0.0, 0.5	0.435, 0.902, 1.0	0.0, 0.134, 1.0	0.128, 0.529, 1.0
$(\min_n B_2(t_n), \mathcal{G}_n[B_2(t_n)], \max_n B_2(t_n)), \%$	0.0, 0.0, 0.506	0.5, 0.942, 1.0	0.5, 0.942, 1.0	0.0, 0.548, 1.0	0.315, 0.686, 1.0
$(\min_n \frac{\mathbb{G}(t_n)}{W}, \frac{\mathbb{E}_n[\mathbb{G}(t_n)]}{W}, \max_n \frac{\mathbb{G}(t_n)}{W}), \text{ bps}$	2.35, 2.86, 2.94	2.08, 2.68, 2.75	1.40, 1.48, 2.11	1.0, 1.89, 2.37	2.28, 2.68, 2.78
UAV 1 Energy Sustainable	No	No	Yes	No	Yes
UAV 2 Energy Sustainable	No	Yes	Yes	No	Yes

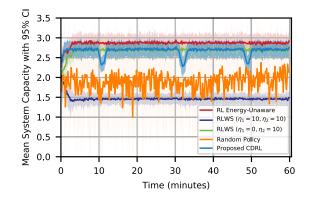


Fig. 7. Performance comparison of the proposed CDRL algorithm with baseline policies. The proposed CDRL agent learns an adaptive feasible policy which achieves a temporal average network capacity that is 81% higher than that of a feasible DRL agent with reward shaping (RLWS ($\eta_1 = \eta_2 = 10$)), and only 6.7% lower than the upper bound achieved by the RL Energy-Unaware agent.

unconstrained PPO agent that penalizes energy dissipation due to flight via fixed reward shaping (RLWS), where the training reward signal is $\hat{\mathcal{R}}(s_n, a_n, \eta) = \mathcal{R}(s_n, a_n) - \eta_1 \mathcal{C}_1(s_n, a_n) - \eta_2 \mathcal{C}_$ $\eta_2 C_2(s_n, a_n)$, and $\eta_1 = 10, \eta_2 = 10$ or $\eta_1 = 0, \eta_2 = 10$, and 3) a random management policy. The achieved mean total network capacity with 95% confidence interval versus flight time based on these policies is shown in Figure 7. The statistical results are based on 32 roll-outs of the learned policy in the simulated wireless IoT environment with NOMA. Compared with baseline policies, it can be seen that the proposed CDRL agent learns an adaptive policy which achieves a temporal average network capacity that is 81%higher compared to the feasible energy sustainable policy learned by the conservative RLWS agent with $\eta_1 = \eta_2 = 10$. Compared to the policy learned by the (RL Energy-Unaware) agent which provides an upper bound on the achievable wireless network capacity, only 6.7% of the system capacity is sacrificed in order to maintain energy sustainability of UAVs. In Table II, we provide statistics which characterize the flight-time of the learned policies to explain their behaviour. Specifically, the minimum flying altitude $\min_n z_m(t_n)$, geometric mean of the altitude during flight $\mathcal{G}_m[z_m(t_n)] =$ $\left(\prod_{n=1}^{H} z_m(t_n)\right)^{\frac{1}{H}}$, and the maximum flying altitude $\max_n z_m(t_n)$, for $m = \{1, 2\}$, are given. These statistics help explain the trade-off between energy sustainability and the achievable wireless network capacity. Notice that the policy learned by the RLWS agent with $\eta_1 = \eta_2 = 10$ is the most

conservative. In this policy, both UAVs climb upwards and hover above the cloud cover to maintain high battery energy throughout the flight. This can be inferred by looking at the temporal geometric mean of the UAV altitude and normalized battery energy during the flight. Such a policy however, results in a poor wireless network capacity with an average of 1.48Wbit per second (bps) due to large scale fading. The behavior of this policy can be justified by noting that the choice of high penalty multipliers make energy dissipation the dominant part in the reward signal. Thus, to maximize the total rewards, the agent will attempt to minimize energy dissipation, which can be achieved by hovering above the cloud cover. On the other hand, the (RL Energy-Unaware) agent learns a policy which is indifferent to battery energy. In this policy, both UAVs descend and hover close to the minimum allowable altitude in order to maximize the achieved system capacity. Notice how the temporal geometric mean of the normalized battery energy attained by this policy is 0. This is because the geometric mean is proportional to the multiplication of the normalized battery energy at each time step, and so if at any time step the normalized battery energy is 0, so will be the geometric mean. The RLWS agent with $\eta_1 = 0, \eta_2 = 10$ behaves as expected, UAV 1 is indifferent to its energy dissipation, hovering close to the minimum allowable altitude to maximize wireless network capacity, where as UAV 2 hovers above the cloud cover to maintain high battery energy throughout the flight, thus minimizing energy dissipation. These experiments demonstrate that choosing the set of Lagrange penalty multipliers to obtain the desired results can be a tedious task. In contrast, the proposed CDRL agent automatically adapts the Lagrange penalty multipliers to maximize the rewards and satisfy the constraints. The policy learned by the proposed CDRL agent indeed strikes a balance; it ensures energy sustainability while slightly sacrificing the network capacity performance.

Policy Generalizability: To demonstrate the generalizability and robustness of the learned CDRL policy, we test its performance on networks with different initial states and massive number of IoT devices. The ability to transfer pre-trained models on small scale networks to larger scale networks is desirable because it is very promising for scalable network management, can amortize the cost of training the RL agent, and addresses sampling complexity issues which arise in larger systems. Recall that the CDRL policy has been trained given that 200 IoT devices are uniformly deployed on ground,

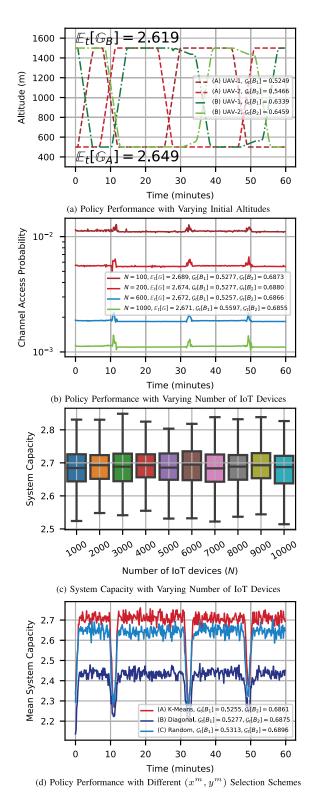


Fig. 8. Learned policy generalizability with varying initial states and network scale. The proposed CDRL agent has been train on a network deployment of N = 200 IoT devices, yet the learned policy can efficiently manage networks with with different initial states and massive number of IoT devices.

and that the two UAVs are initially present at altitudes of 250m and 750m. In Figure 8(a), we demonstrate the learned policy performance given different initial altitudes of UAVs. Specifically, we consider two extreme cases: both UAVs are initially deployed at the altitude of 500m (case A), or at 1500m

(case B). For those two cases, Figure 8(a) shows that the two UAVs tend to fully de-synchronize their vertical flight trajectories, such that when one of them is charging its battery at 1500m, the other is provisioning wireless service at 500m. The temporal average system capacity for cases A and B are 2.649W bps and 2.619W bps, respectively. Notice that case B achieves a slightly lower temporal average network capacity because both UAVs are initially farther away from IoT devices. In the legend, the temporal geometric mean of the battery energy of each UAV is reported to demonstrate energy sustainability of UAVs throughout the operating horizon.

In Figure 8(b), we test how the learned CDRL policy scales with varying number of IoT devices. As can be seen from Figure 8(b), the channel access probability is scaled appropriately given the number of IoT devices vary in $\{100, 200, 600, 1000\}$, maintaining comparable temporal average network capacity around 2.67W bps. In addition, the temporal geometric mean of the battery energy of each UAV is also reported in the legend to demonstrate energy sustainability of UAVs. In Figure 8(c), we plot a boxplot of the achieved system capacity for massive deployments of IoT devices up to 10000 users. It can be seen that the learned policy network maintains high performance which is not compromised by increasing the number of IoT devices. Last but not least, in Figure 8(d), we test the performance of the learned policy given different horizontal deployment of the two UAVs. We consider three cases: (A) the two UAVs are deployed at (250, 250)m and (750, 250)m, as determined by the K-means clustering algorithm, (B) the two UAVs are deployed farthest from each other at (0,0)m and (1000,500)m, and (C) the two UAVs are randomly deployed on the xy-plane. It can be observed from Figure 8(d) that the mean network capacity is highest when the K-means algorithm is employed to determine the xy-planar deployment of the two UAVs. In addition, it is shown that randomly deploying the two UAVs in the xy-plane, case (C), achieves a mean network capacity which is slightly $(\approx 2\%)$ lower than that in case (A), whereas the extreme case of deploying the two UAVs on the diagonal, case (B), achieves the lowest network capacity ($\approx 10\%$ lower compared to that of case (A)). These results support our argument that the range of vertical flight is the dominant factor in our system model, and hence determining the planar locations of UAVs a priori reduces the number of control variables without adversely impacting network performance. In all cases, the learned policy still ensures energy sustainability of the two UAVs as indicated by the temporal geometric mean of the battery energy of each UAV, which is reported in the legend.

VI. CONCLUSION

In this paper, we study the joint problem of dynamic multi-UAV altitude control and random channel access management of a multi-cell UAV-based wireless network with NOMA, in support of a massive number of IoT devices. To enable an energy-sustainable capacity-optimal IoT network, we have formulated this constrained stochastic control problem as a constrained markov decision process, and proposed an online model-free constrained deep reinforcement learning algorithm to learn an optimal control policy for wireless network management. Our extensive simulations have demonstrated that the proposed algorithm outperforms baseline solutions, and learns a cooperative policy in which the altitude of UAVs and channel access probability of IoT devices are dynamically adapted to maximize the long-term total network capacity while ensuring energy sustainability of UAVs. In our future work, we will build a testbed in order to investigate data-driven control of wireless networks based on real hardware and real data.

ACKNOWLEDGMENT

The authors would like to thank the computing resources provided on Bebop, a high-performance computing cluster operated by the Laboratory Computing Resource Center at Argonne National Laboratory.

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